Scheme of Learning



#MathsEveryoneCan





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Welcome

Nhite Røse

Welcome to the White Rose Maths' new, more detailed schemes of learning for 2018-19.

We have listened to all the feedback over the last 2 years and as a result of this, we have made some changes to our primary schemes. *They are bigger, bolder and more* detailed than before.

The new schemes still have the *same look and feel* as the old ones, but we have tried to provide more detailed guidance. We have worked with enthusiastic and passionate teachers from up and down the country, who are experts in their particular year group, to bring you additional guidance. *These schemes have been written* for teachers, by teachers.

We all believe that every child can succeed in

mathematics. Thank you to everyone who has contributed to the work of White Rose Maths. It is only with your help that we can make a difference.

We hope that you find the new schemes of learning helpful. As always, get in touch if you or your school want support with any aspect of teaching maths.

If you have any feedback on any part of our work, do not hesitate to contact us. Follow us on Twitter and Facebook to keep up-to-date with all our latest announcements.

White Rose Maths Team #MathsEveryoneCan

White Rose Maths contact details



<u>Support@whiterosemaths.com</u>



@WhiteRoseMaths

White Rose Maths

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What's included?

Our schemes include:

- Small steps progression. These show our blocks broken down into smaller steps.
- Small steps guidance. For each small step we provide some brief guidance to help teachers understand the key discussion and teaching points. This guidance has been written for teachers, by teachers.
- A more integrated approach to fluency, reasoning and problem solving.
- Answers to all the problems in our new scheme.
- We have also worked with Diagnostic Questions to provide questions for every single objective of the National Curriculum.

Teaching Notes and Examples



Answers to Reasoning Questions



Overview Small Steps Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and write numbers in numerals and words Controletes to 100 and read and more numbers in numerals and words Controletes to 100 and read and more numbers in numerals and words Controletes to 100 and read and to 100 and 100 an



Meet the Team

The schemes have been developed by a wide group of passionate and enthusiastic classroom practitioners.



Special Thanks

The White Rose Maths team would also like to say a huge thank you to the following people who came from all over the country to contribute their ideas and experience. We could not have done it without you.

Year 2 Team

Chris Gordon Beth Prottey Rachel Wademan Emma Hawkins Scott Smith Valda Varadinek-Skelton Chloe Hall Charlotte James Joanne Stuart Michelle Cornwell

Year 3 Team

Becky Stanley Nicola Butler Laura Collis Richard Miller Claire Bennett Chris Conway

Year 4 Team

Terrie Litherland Susanne White Hannah Kirkman Daniel Ballard Isobel Gabanski Laura Stubbs

Year 5 Team

Lynne Armstrong Laura Heath Clare Bolton Helen Eddie Chris Dunn Rebecca Gascoigne

Year 6 Team

Lindsay Coates Kayleigh Parkes Shahir Khan Sarah Howlett







How to use the small steps

We were regularly asked how it is possible to spend so long on particular blocks of content and National Curriculum objectives.

We know that breaking the curriculum down into small manageable steps should help children understand concepts better. Too often, we have noticed that teachers will try and cover too many concepts at once and this can lead to cognitive overload. In our opinion, it is better to follow a small steps approach.

As a result, for each block of content we have provided a "Small Step" breakdown. We recommend that the steps are taught separately and would encourage teachers to spend more time on particular steps if they feel it is necessary. Flexibility has been built into the scheme to allow this to happen.

Teaching notes

Alongside the small steps breakdown, we have provided teachers with some brief notes and guidance to help enhance their teaching of the topic. The "Mathematical Talk" section provides questions to encourage mathematical thinking and reasoning, to dig deeper into concepts.

We have also continued to provide guidance on what varied fluency, reasoning and problem solving should look like.





Assessments

Alongside these overviews, our aim is to provide an assessment for each term's plan. Each assessment will be made up of two parts:

Part 1: Fluency based arithmetic practice

Part 2: Reasoning and problem solving based questions

Teachers can use these assessments to determine gaps in children's knowledge and use them to plan support and intervention strategies.

The assessments have been designed with new KS1 and KS2 SATs in mind.

For each assessment we provide a summary spread sheet so that schools can analyse their own data. We hope to develop a system to allow schools to make comparisons against other schools. Keep a look out for information next year.



White R©se Maths

Teaching for Mastery

These overviews are designed to support a mastery approach to teaching and learning and have been designed to support the aims and objectives of the new National Curriculum.

The overviews:

- have number at their heart. A large proportion of time is spent reinforcing number to build competency
- ensure teachers stay in the required key stage and support the ideal of depth before breadth
- ensure students have the opportunity to stay together as they work through the schemes as a whole group
- provide plenty of opportunities to build reasoning and problem solving elements into the curriculum

For more guidance on teaching for mastery, visit the NCETM website:

https://www.ncetm.org.uk/resources/47230

Concrete - Pictorial - Abstract

We believe that all children, when introduced to a new concept, should have the opportunity to build competency by taking this approach.

Concrete – children should have the opportunity to use concrete objects and manipulatives to help them understand what they are doing.

Pictorial – alongside this children should use pictorial representations. These representations can then be used to help reason and solve problems.

Abstract – both concrete and pictorial representations should support children's understanding of abstract methods.

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Need some CPD to develop this approach? Visit <u>www.whiterosemaths.com</u> for find a course right for you.

Training

White Rose Maths offer a plethora of training courses to help you embed teaching for mastery at your school.

Our popular JIGSAW package consists of five key elements:

- CPA
- Bar Modelling
- Mathematical Talk & Questioning
- Planning for Depth
- Reasoning & Problem Solving



For more information and to book visit our website <u>www.whiterosemaths.com</u> or email us directly at <u>support@whiterosemaths.com</u>







Additional Materials

In addition to our schemes and assessments we have a range of other materials that you may find useful.

KS1 and KS2 Problem Solving Questions

For the last three years, we have provided a range of KS1 and KS2 problem solving questions in the run up to SATs. There are over 200 questions on a variety of different topics and year groups. You will also find more questions from our Barvember campaign.



End of Block Assessments

New for 2018 we are providing short end of block assessments for each year group. The assessments help identify any gaps in learning earlier and check that children have grasped concepts at an appropriate level of depth.







FAQs

If we spend so much time on number work, how can we cover the rest of the curriculum?

Children who have an excellent grasp of number make better mathematicians. Spending longer on mastering key topics will build a child's confidence and help secure understanding. This should mean that less time will need to be spent on other topics.

In addition, schools that have been using these schemes already have used other subjects and topic time to teach and consolidate other areas of the mathematics curriculum.

Should I teach one small step per lesson?

Each small step should be seen as a separate concept that needs teaching. You may find that you need to spend more time on particular concepts. Flexibility has been built into the curriculum model to allow this to happen. This may involve spending more or less than one lesson on a small step, depending on your class' understanding.

How do I use the fluency, reasoning and problem solving questions?

The questions are designed to be used by the teacher to help them understand the key teaching points that need to be covered. They should be used as inspiration and ideas to help teachers plan carefully structured lessons.

How do I reinforce what children already know if I don't teach a concept again?

The scheme has been designed to give sufficient time for teachers to explore concepts in depth, however we also interleave prior content in new concepts. E.g. when children look at measurement we recommend that there are lots of questions that practice the four operations and fractions. This helps children make links between topics and understand them more deeply. We also recommend that schools look to reinforce number fluency through mental and oral starters or in additional maths time during the day.



Meet the Characters

Children love to learn with characters and our team within the scheme will be sure to get them talking and reasoning about mathematical concepts and ideas. Who's your favourite?





	Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8	Week 9	Week 10	Week 11	Week 12
Number: Place Value			Number: Addition and Subtraction					Number: Multiplication and Division			Consolidation	
Spring	Number: Multiplication and Division			Measurement: Money	Stati	istics	Measu an	rement: l d Perime	Length ter	Num Frac	nber: tions	Consolidation
Summer	Number: Fractions		Meas	urement:	Time	Geon Proper Sha	netry: rties of ape	Measur	ement: M Capacity	lass and	Consolidation	



Year 3 | Spring Term | Week 1 to 3 – Number: Multiplication & Division



Overview Small Steps

	-
Comparing statements	
Related calculations	
Multiply 2-digits by 1-digit (1)	
Multiply 2-digits by 1-digit (2)	
Divide 2-digits by 1-digit (1)	
Divide 2-digits by 1-digit (2)	
Divide 2-digits by 1-digit (3)	
Scaling	
How many ways?	

NC Objectives

Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables.

Write and calculate mathematical statements for multiplication and division using the multiplication tables they know, including for twodigit numbers times one-digit numbers, using mental and progressing to formal written methods.

Solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.



Comparing Statements

Notes and Guidance

Children use their knowledge of multiplication and division facts to compare statements using inequality symbols.

It is important that children are exposed to a variety of representations of multiplication and division, including arrays and repeated addition.

Varied Fluency







Use <, > or = to compare.







Complete the number sentences.



Mathematical Talk

What other number sentences does the array show?

If you know your 4 times-table, how can you use this to work out your 8 times-table?

What's the same and what's different about 8 \times 3 and 7 \times 4?

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Comparing Statements

Whitney says, 8×8 is greater than two lots of 4×8 Do you agree? Can you prove your answer?	Possible answer: She is wrong because they are equal.	Can you find three different ways to complete each number sentence? $ _ \times 3 + _ \times 3 < _ \div 3$ $ _ \div 4 < _ \times 4 < _ \times 4$ $ _ \times 8 > _ \div 8 > _ \times 8$	Possible answers include: $1 \times 3 + 1 \times 3 < 21 \div 3$ $1 \times 3 + 1 \times 3 < 24 \div 3$ $1 \times 3 + 1 \times 3 < 27 \div 3$ $24 \div 4 < 8 \times 4 < 12 \times 4$ $16 \div 4 < 5 \times 4 < 7 \times 4$ $8 \div 4 < 3 \times 4 < 4 \times 4$ $4 \times 8 > 88 \div 8 > 1 \times 8$ $2 \times 8 > 80 \div 8 > 1 \times 8$ $6 \times 8 > 96 \div 8 > 1 \times 8$
True or false?			
6 × 7 < 6 + 6 + 6 + 6 + 6 + 6 + 6	False		
$7 \times 6 = 7 \times 3 + 7 \times 3$	True		
2 × 3 + 3 > 5 × 3	False		



Related Calculations

Notes and Guidance

- Children use known multiplication facts to solve other multiplication problems.
- They understand that because one of the numbers in the calculation is ten times bigger, then the answer will also be ten times bigger.
- It is important that children develop their conceptual understanding through the use of concrete manipulatives.

Mathematical Talk

- What is the same and what is different about the place value counters?
- How does this fact help us solve this problem?
- If we know these facts, what other facts do we know?
- Can you prove your answer using manipulatives?

Varied Fluency



If each hole is worth ten, what do the pieces represent?

- If we know $2 \times 6 = 12$, we also know $2 \times 60 = 120$ Use this to complete the fact family.



Complete the fact families for the calculations.





Related Calculations

I know that when multiplying 3 by 40, 40 is ten times bigger than 4, so my answer will be ten times bigger than 3 × 4 Is Mo correct? Explain your answer.	Mo is correct. I know $3 \times 4 = 12$, so if he has $3 \times$ 40 then his answer will be ten times bigger because 4 has become ten times bigger.	True or false? $5 \times 30 = 3 \times 50$ Prove it.	Possible response: Children may represent it with place value counters. True because they are equal.
Rosie has 240 cakes to sell. She puts the same number of cakes in each box and has no cakes left over. Which of these boxes could she use?	She could use 10, 20, 30, 40, 60, 80 because 240 is a multiple of all of these numbers. $10 \times 24 = 240$ $20 \times 12 = 240$ $30 \times 8 = 240$ $40 \times 6 = 240$ $60 \times 4 = 240$ $80 \times 3 = 240$		Children may explore the problem in a context. e.g. 5 lots of 30 apples compared to 3 lots of 50 apples.



Multiply 2-digits by 1-digit (1)

Notes and Guidance

Children use their understanding of repeated addition to represent a two-digit number multiplied by a one-digit number with concrete manipulatives. They use the formal method of column multiplication alongside the concrete representation. They also apply their understanding of partitioning to represent and solve calculations.

In this step, children explore multiplication with no exchange.

Mathematical Talk

How does multiplication link to addition?

How does partitioning help you to multiply 2-digits by a 1-digit number?

How does the written method match the concrete representation?

Varied Fluency

There are 21 coloured balls on a snooker table. How many coloured balls are there on 3 snooker tables?

Use Base 10 to calculate: 21×4 and 33×3



Complete the calculations to match the place value counters. Tens Ones 1 1 1 (1)1



Т

3

6

0

4

2

8







Multiply 2-digits by 1-digit (1)





Multiply 2-digits by 1-digit (2)

Notes and Guidance

Children continue to use their understanding of repeated addition to represent a two-digit number multiplied by a onedigit number with concrete manipulatives.

They move on to explore multiplication with exchange. Each question in this step builds in difficulty.

Varied Fluency

Т 0

2

9 6



	Use Jack's method to solve:	
	13 × 4	
1	23 × 4	
	26 × 3	

Mathematical Talk

What happens when we have ten or more ones in a column? What happens when we have twenty or more ones in a column?

How do we record our exchange?

Do you prefer Jack's method or Amir's method? Can you use either method for all the calculations?





Multiply 2-digits by 1-digit (2)

Always, Sometimes, Never? A two-digit number multiplied by a one-digit number has a two-digit product.		Sometimes. e.g. $13 \times 5 = 65$ $31 \times 5 = 155$		How close can you get to 100? Use each digit card once in the multiplication.	You can get within 8 of 100 $23 \times 4 = 92$ this is the closest answer. $24 \times 3 = 72$ $32 \times 4 = 128$			
Explain the mistake.		They have not			$34 \times 2 = 68$			
Н Т О		performed the exchange						
	2 7		correctly. 6 tens and 2 tens					
	×		3		should be added			
	6	2	1		8 tens so the correct answer is 81			



Divide 2-digits by 1-digit (1)

Notes and Guidance

Children divide 2-digit numbers by a 1-digit number by partitioning into tens and ones and sharing into equal groups.

They divide numbers that do not involve exchange or remainders.

It is important that children divide the tens first and then the ones.

Mathematical Talk

How can we partition the number? How many tens are there? How many ones are there? What could we use to represent this number? How many equal groups do I need?

How many rows will my place value chart have? How does this link to the number I am dividing by?

Varied Fluency

Ron uses place value counters to solve 84 \div 2



I made 84 using place value counters and divided them between 2 equal groups.

 $66 \div 3$



Use Ron's method to calculate:

84 ÷ 4



Eva uses a place value grid and part-whole model to solve $66 \div 3$

 $66 \div 2$





Use Eva's method to calculate:

69 ÷ 3	96 ÷ 3	86 ÷ 2



Divide 2-digits by 1-digit (1)





Divide 2-digits by 1-digit (2)

Notes and Guidance

Children divide 2-digit numbers by a 1-digit number by partitioning into tens and ones and sharing into equal groups.

They divide numbers that involve exchanging between the tens and ones. The answers do not have remainders.

Children use their times-tables to partition the number into multiples of the divisor.

Mathematical Talk

Why have we partitioned 42 into 30 and 12 instead of 40 and 2?

What do you notice about the partitioned numbers and the divisor?

Why do we partition 96 in different ways depending on the divisor?

Varied Fluency

Ron uses place value counters to divide 42 into three equal groups.



He shares the tens first and exchanges the remaining ten for ones.

> Then he shares the ones. $42 \div 3 = 14$

Use Ron's method to calculate 48 \div 3 , 52 \div 4 and 92 \div 8

Annie uses a similar method to divide 42 by 3

Tens	Ones
1 0	
10	0 0 0 0
•	

Use Annie's method to calculate:

 $96 \div 8$ $96 \div 4$ $96 \div 3$ $96 \div 6$



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Divide 2-digits by 1-digit (2)





Divide 2-digits by 1-digit (3)

Notes and Guidance

Children move onto solving division problems with a remainder.

Links are made between division and repeated subtraction, which builds on learning in Year 2

Children record the remainders as shown in Tommy's method. This notation is new to Year 3 so will need a clear explanation.

Mathematical Talk

How do we know 13 divided by 4 will have a remainder?

Can a remainder ever be more than the divisor?

Which is your favourite method? Which methods are most efficient with larger two digit numbers?

Varied Fluency

How many squares can you make with 13 lollipop sticks?

There are ____ lollipop sticks.

There are ____ groups of 4

There is ____ lollipop stick remaining.

13 ÷ 4 = ____ remainder ____

Use this method to see how many triangles you can make with 38 lollipop sticks.

Tommy uses repeated subtraction to solve
$$31 \div 4$$

 $\int_{0}^{-4} \int_{7}^{-4} \int_{11}^{-4} \int_{15}^{-4} \int_{19}^{-4} \int_{23}^{-4} \int_{27}^{-4} \int_{31}^{-4} \int_{7}^{-4} \int_{$

Use Tommy's method to solve 38 divided by 3

Use place value counters to work out 94 ÷ 4 Did you need to exchange any tens for ones? Is there a remainder?



Tens	Ones



Divide 2-digits by 1-digit (3)

Reasoning and Problem Solving

Which calculation is the odd one out? Explain your thinking.



64 ÷ 8 could be the odd one out as it is the only calculation without a remainder.

Make sure other answers are considered such as $65 \div 3$ because it is the only one being divided by an odd number.



He sorts his stickers into equal groups but has some stickers remaining. How many stickers could be in each group and how many stickers would be remaining?

Dora and Eva are planting bulbs. They have 76 bulbs altogether.

Dora plants her bulbs in rows of 8 and has 4 left over. Eva plants her bulbs in rows of 10 and has 2 left over.

How many bulbs do they each have?

There are many solutions, encourage a systematic approach. e.g. 2 groups of 7, remainder 1 3 groups of 4, remainder 3 2 groups of 6, remainder 3

Dora has 44 bulbs. Eva has 32 bulbs.



Scaling

Notes and Guidance

- It is important that children are exposed to problems involving scaling from an early age.
- Children should be able to answer questions that use the vocabulary "times as many".
- Bar models are particularly useful here to help children
- visualise the concept. Examples and non-examples should be used to ensure depth of understanding.

Mathematical Talk

- Why might someone draw the first bar model? What have they misunderstood?
- What is the value of Amir's counters? How do you know?
- How many adults are at the concert? How will you work out the total?

Varied Fluency

/ In a playground there are 3 times as many girls as boys.



Which bar model represents the number of boys and girls? Explain your choice.

Praw a bar model to represent this situation.

In a car park there are 5 times as many blue cars as red cars.

• Eva has these counters



Amir has 4 times as many counters. How many counters does Amir have?

There are 35 children at a concert.
 3 times as many adults are at the concert.
 How many people are at the concert in total?



Scaling

Reasoning and Problem Solving

Dora says Mo's tower is 3 times taller than her tower.

Mo says his tower is 12 times taller than Dora's tower. Who do you agree with? Explain why?



I agree with Dora. Her tower is 4 cubes tall. Mo's tower is 12 cubes tall. 12 is 3 times as big as 4. Mo has just counted his cubes and not compared them to Dora's tower. In a playground there are 3 times as There are 10 boys in the playground. many girls as boys. There are 30 girls. Label and complete the bar model to boys 10 help you work out how many boys there girls 10 10 10 are in the playground. 30 A box contains some counters. There are 6 pink There are twice as many green counters counters. as pink counters. There are 18 counters in total. How many pink counters are there?



How Many Ways?

Notes and Guidance

Children list systematically the possible combinations resulting from two groups of objects. Encourage the use of practical equipment and ensure that children take a systematic approach to each problem.

Children should be encouraged to calculate the total number of ways without listing all the possibilities. e.g. Each T-shirt can be matched with 4 pairs of trousers so altogether $3 \times 4 = 12$ outfits.

Mathematical Talk

What are the names of the shapes on the shape cards? How do you know you have found all of the ways? Would making a table help?

Without listing, can you tell me how many possibilities there would be if there are 5 different shape cards and 4 different number cards?

Varied Fluency

Jack has 3 T-shirts and 4 pairs of trousers. Complete the table to show how many different outfits he can make.



T-shirt	Trousers
Blue	Blue
Blue	Dark blue
Blue	Orange
Blue	Green



\frown	\square	\square	\frown	\frown	\frown	\square
				1	2	7
\square						

She chooses a shape card and a number card. List all the possible ways she could do this.



How Many Ways?

